



Introduction

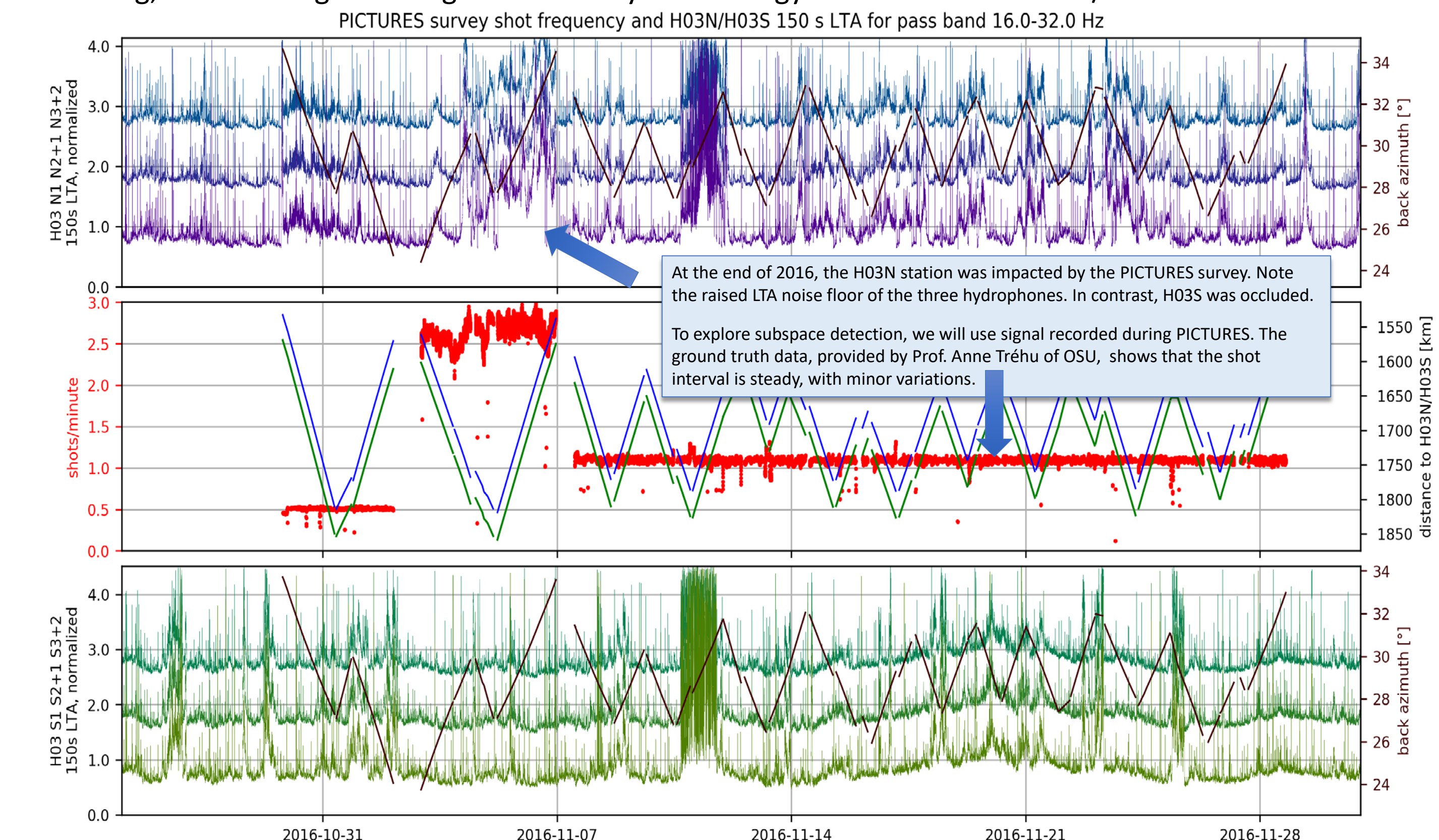
Marine seismic surveys make use of a ship-towed air-gun array. The compressed-air shots fired into the water generate impulsive sound wave fronts whose reflections are recorded to map the oceanic crust. These intense sounds cause depletion of the local zooplankton [1], and can impact the detection capability of the CTBTO hydroacoustic stations and their automated processing [2].

It is desirable to detect the presence of these surveys, also when at great remove and low SNR. To this end, we explore adaptation of the subspace detection method [3] from seismology to hydroacoustics. In implementing the requisite algorithms, use was made of the ObsPy Python framework [4].

Subspace detection [3] involves computing an orthonormal basis from signal templates through singular value decomposition. The signal subspace spanned by the first few such basis vectors will capture the most common template characteristics. Projecting signal onto this subspace will yield significant coefficients (detection) when the signal resembles the templates.

The signal projection operation is equivalent to cross correlation with each of the basis vectors. When the dimension of the basis is 1, the procedure reduces to cross correlating with a single template (matched filtering).

Subspace detection is able to accommodate an adjustable wider variation of signals than matched filtering, while having much higher sensitivity than energy detectors such as STA/LTA.

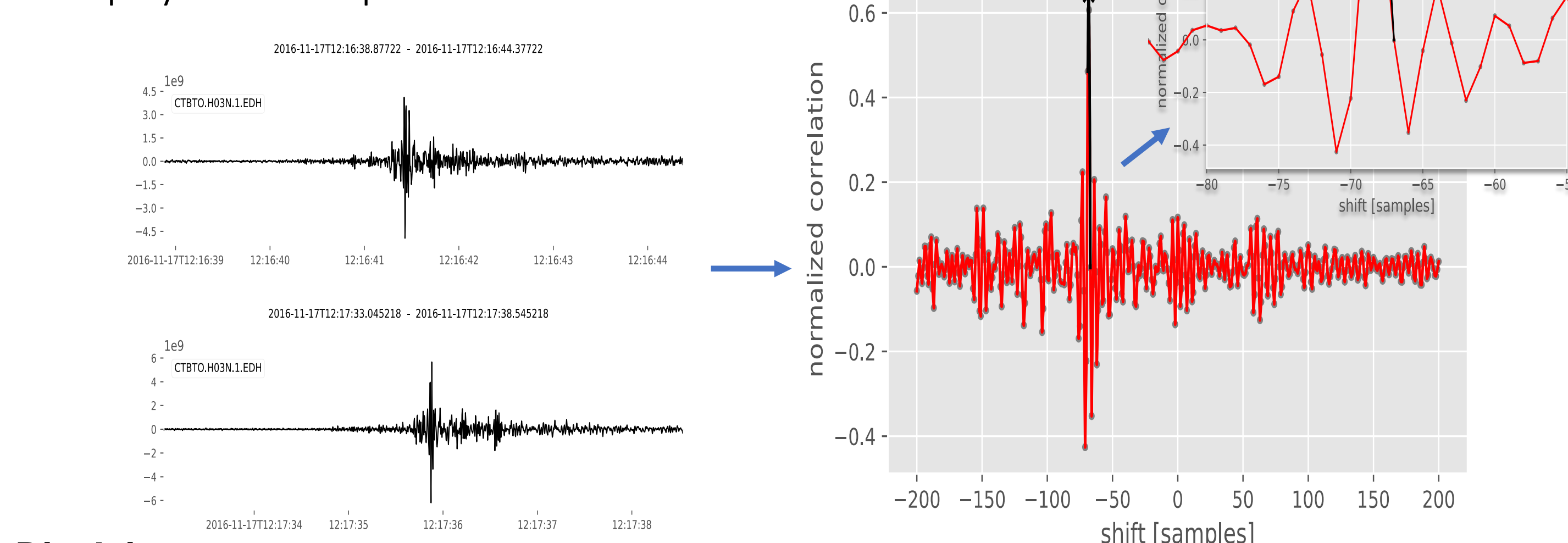


To construct a subspace detector, it is required to select and extract aligned signal templates from which to compute the basis. Since air gun survey shots manifest as impulsive hydroacoustic signals, the logical approach is to obtain templates from shot signals. Raw hydroacoustic data was obtained from the CTBTO [Virtual Data Exploitation Centre](#), detrended, and 5-80 Hz band pass filtered prior to further processing.

Extracting templates

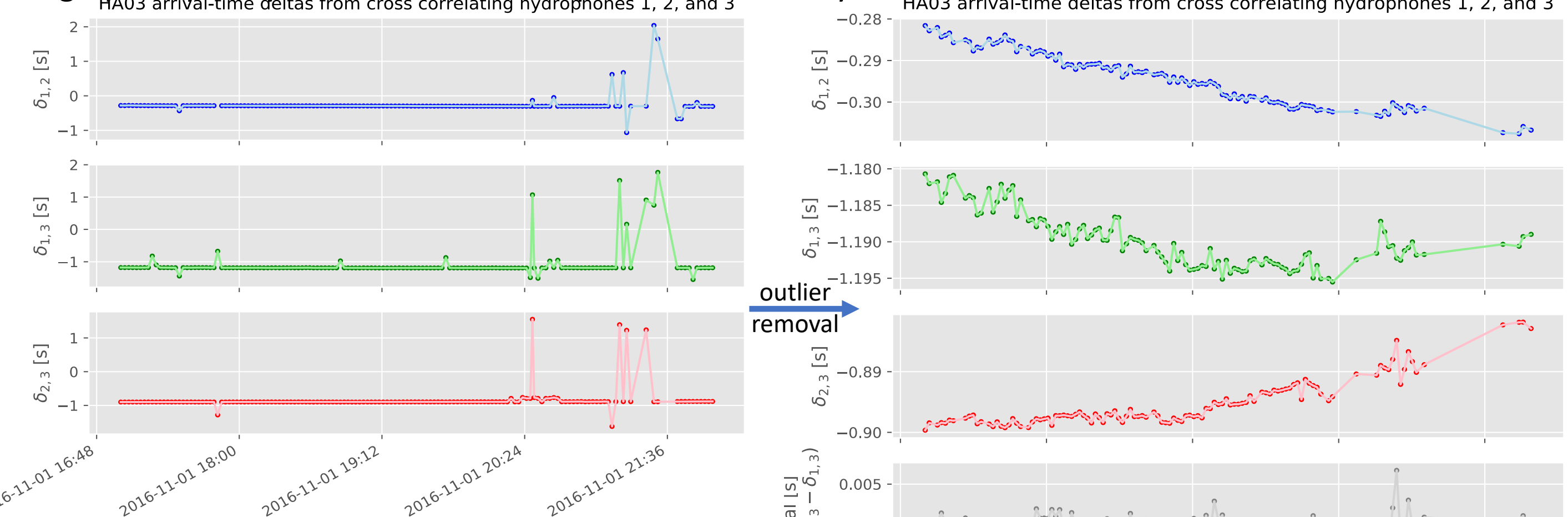
The traces of all three hydrophones are subjected to a shot-tuned 1s/8s recursive STA/LTA trigger from which pick-on and pick-off times as well as an SNR measure are obtained. Picks coincident (within 2.5s) for all three hydrophones are marked as candidate shots. Trace slices are cut around these picks (see for example below), but these are only very roughly shot-phase aligned.

Auto and cross correlation is used to refine the arrival time delay between different shots, and of a given shot between hydrophones. To gain sub-sample precision in these time deltas, the point with maximum correlation coefficient and its two neighbours are interpolated with their uniquely-determined parabola.



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A survey hypothesis can be automatically established by collecting coincident arrivals with similar inter-hydrophone arrival time deltas: an ongoing survey can be assumed to be the predominant source of arrivals, and to have a slowly changing back azimuth and hence slowly changing deltas. This is done through iterative joint outlier removal. If this retains a large fraction of the coincident arrivals, a survey is highly likely. Only these arrivals are kept for further analysis.



The residual $\delta_{1,2} + \delta_{2,3} - \delta_{1,3}$ of the delta measurements should be close to zero since for the true arrival times, the equality $(t_2 - t_1) + (t_3 - t_2) - (t_3 - t_1) = 0$ holds. This provides a sanity check. Note the sub-sample-period (0.004s) precision.

To align hydrophone traces such that arrivals of the same shot from the survey coincide, values for $\delta_{1,2}$ and $\delta_{1,3}$ as a function of time are needed, with hydrophone 1 serving as a reference.

Instead of directly using the $\delta_{1,2}$ and $\delta_{1,3}$ values for this, a better result can be obtained by making use of both the $\delta_{2,3}$ measurements and the fact that without measurement error, $\delta_{1,2} + \delta_{2,3} - \delta_{1,3} = 0$. This is done via a least squares solution for $\delta_{1,2}^{i,s}$ and $\delta_{1,3}^{i,s}$ to the set of equations

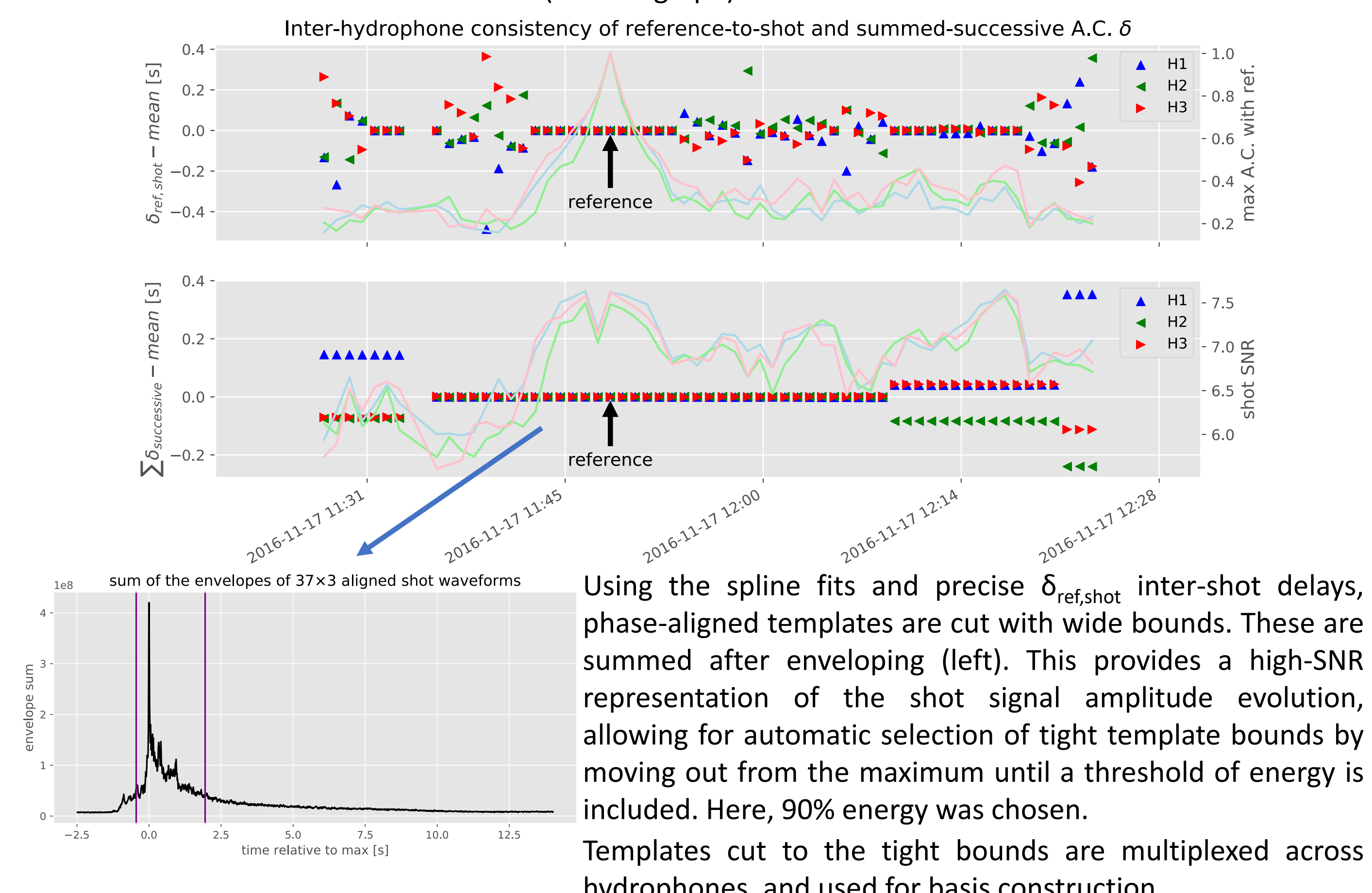
$$\delta_{1,2}^{i,s} = \delta_{1,2}^{i,s, \text{meas}}, \delta_{1,3}^{i,s} = \delta_{1,3}^{i,s, \text{meas}}, -\delta_{1,2}^{i,s} + \delta_{1,3}^{i,s} + \delta_{2,3}^{i,s} = \delta_{2,3}^{i,s, \text{meas}}$$

for every arrival (shot) i in the survey subset. The result, shown in the plot to the right, is subtly different from the measured $\delta_{1,2}$ and $\delta_{1,3}$ values shown on the previous slide. Further precision and a piecewise analytical representation of $\delta_{1,2}(t)$ and $\delta_{1,3}(t)$ are obtained through cubic spline fits to the $\delta_{1,2}^{i,s}$ and $\delta_{1,3}^{i,s}$ values.

The smoothing is adjustable, and in the example above has been set to a 6 points per spline knot (the + symbols) target.

To align different arrivals on the same hydrophone, as required for template extraction, the precise time deltas between arrivals/shots (with outliers removed) must be determined. Two methods are tried:

- direct reference-to-shot auto-correlation (top graph)
- summed-successive auto-correlation (bottom graph).



Using the spline fits and precise $\delta_{\text{ref,shot}}$ inter-shot delays, phase-aligned templates are cut with wide bounds. These are summed after enveloping (left). This provides a high-SNR representation of the shot signal amplitude evolution, allowing for automatic selection of tight template bounds by moving out from the maximum until a threshold of energy is included. Here, 90% energy was chosen. Templates cut to the tight bounds are multiplexed across hydrophones, and used for basis construction.

Subspace detection

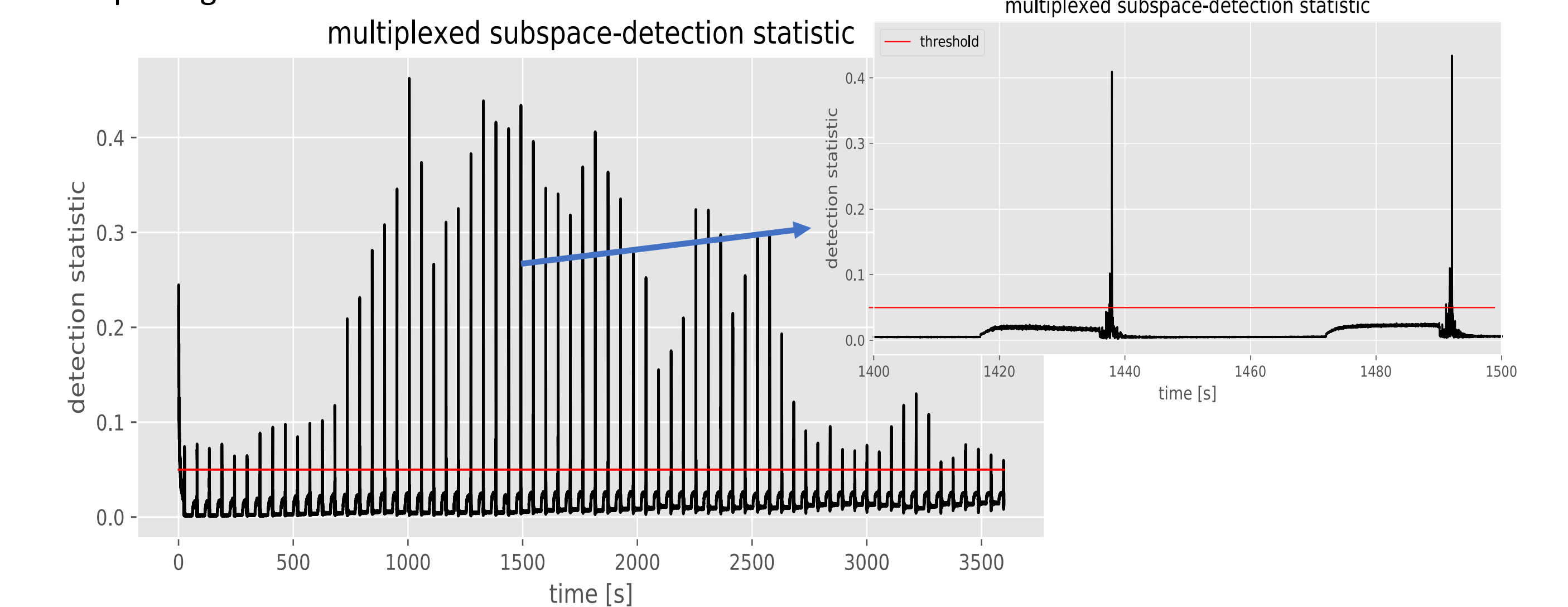
After singular value decomposition of a matrix constructed from multiplexed tight templates, a U matrix results with orthogonal column vectors that can be used as basis vectors for a signal subspace.

The plots to the right show the first eight of these basis vectors in order of decreasing σ value.

An appropriate choice of subspace dimension can be made by reviewing the fraction of energy of the multiplexed templates captured by subspaces of increasing dimension constructed from the basis vectors with highest σ value.

As seen on the right, the first 5 basis vectors are sufficient to capture 50% of the template energy.

Using a modified detection statistic, the so-constructed subspace detector is able to pick out shots with very high sensitivity when applied to a hydrophone-multiplexed signal stream. Though the amplitude of the statistic drops off away from the time period covered by the templates, this is likely partly due to only a single pair of average $\delta_{1,2}$ and $\delta_{1,3}$ phase alignments having been applied to the entire stream prior to multiplexing.



Conclusions

- Subspace detection is a viable method for hydroacoustics.
- Good detection sensitivity was demonstrated.
- A single non-multiplexed subspace constructed from and applied to all three hydrophones should result in slower drop-off.
- Parabola interpolation provides sub-sample-period precision in measuring time delays via auto/cross correlation. This improvement can readily be added to HASE.
- Neither method A nor B tried for determining $\delta_{\text{ref,shot}}$ seems optimal, though B works better. Weighted least-squares optimization using the full correlation matrix is an option.

References

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