



INTRODUCTION

Brain waves are out there carrying thoughts about a unified configuration tool for analysis of seismic data. We mean a multi-task Deep Neural Network (DNN) [Kislov, Gravirov, 2018; Ross et al., 2018; Yuan et al., 2018; Meyer et al., 2019]. Due to the specifics of the seismic data and the range of tasks which cannot be identified in advance a very complex network will be required.

To simplify the network architecture and facilitate its training, it is necessary to carry out the data pre-processing. The STA/LTA method is widely used for it. Other technologies are also known [Gentili, Michelini, 2006; Kislov, Gravirov, 2010; Kislov, Gravirov, 2011]. The second stage depends on the objectives of the analysis. Each time, a new method of data preprocessing is developed. This creates an obstacle to the using of DNN's multi-task.

Thirty numerical parameters are enough to characterize a ten-second seismic recording. If we could measure them correctly, we would the mysteries of the Earth, but not the secrets of signals. If the pre-processing marks out features of a signal and allows it to be viewed in a smaller space, this will simplify the post-processing algorithms and their learning.

It is necessary to create the pre-processing algorithm, which will not lose the informative features of the signal. It can be used in any analysis, but the multi-task DNN is primarily meant.

DATA PRE-PROCESSING METHODS

The data pre-processing includes data formatting, data deletion and/or restoration, extraction of informative features and scaling of the feature vector [Kong et al., 2018; Kotsiantis et al., 2006].

Most of all, we are interested in extracting informative features. For this, signal transformation can be used without dimension reduction [Gravirov et al., 2013]. The way of extraction features can have physical interpretation. This increases the visibility of the method, provides opportunity to control the processing of data. On the other hand, features that do not have a clear physical meaning can provide better recognition capability. The method of data pre-processing should provide:

- noise reduction,
- data compression,
- signal reconstruction without noise,
- the ability to work in a real time.

THE EXTRACTING OF INFORMATIVE FEATURES OF DATA

Let a seismic signal $w_i \in W^{*N}$ has a length of N samples. As a result of the transformation $v_j = f(w_i)$, we get another representation having M counts long, which shows the features of the seismic signal. All set of possible signals W^{*N} is mapped onto a set of representations $V^M = F(W^{*N})$. There is an inverse transform $w_i = g(v_j)$; $W^{*N} = G(V^M)$.

Errors of transformations cause that w_i is slightly different from w_j . This difference should not exceed some value E . First and foremost, the reconstructed signal should show the same seismic event, with the parameters in the corresponding tolerance. The formal procedure for determining the error E , for example, the ordinary least squares technique, is ill-suited here.

Since the original signal contains noise, the real set W exceeds the ideal W^* . In addition we agree with some loss of information at direct transformation in a pursuit of the compact representation of v_j , i.e., close input signals will have the same representation. Direct and inverse transformations have to be stable with rather small disturbances at the inputs. Then the analysis which is carried out in a time domain can be equally possible in the transformation domain.

COMPRESSIVE SAMPLING

Consider a method called Compressed Sensing, Sparse Sampling, or Compressive Sampling (CS). In geophysics, this method has been used for about 40 years [Taylor et al., 1979; Oldenburg et al., 1983; Gan et al., 2016].

Transform the signal $w \in W^N$ into a space of low dimensionality $y_i = \Phi w_i$. Matrix of linear map $\Phi \in M^{*N}$ acts as an encoder. Let's represent the signal via some basis $W = \Psi x$, where the columns of the matrix $\Psi \in M^{*N}$ are the coordinates of the basis Ψ , and column vector $x \in W^N$ contains the coefficients that represent the signal w in the basis Ψ . The representation $x \in W^N$ will be called s -sparse if x is a linear combination of s basis vectors only, i.e. with the condition $\|x\|_0 \leq s$. The vector x is called compressible if the s components are large enough, and the others are small. The CS uses the rule that all natural signals are rare when they are expressed properly [Candès, Wakin, 2008]. When $M < N$, the equation $y - \Phi z = 0$ has an infinite number of solutions z . To restore the original signal, CS uses the information that x is compressible.

The signal coding is a simple linear procedure $y = Ax$, where the measurement matrix $A = \Phi\Psi$ must satisfy the Restricted Isometry Property (RIP). The fulfillment of this condition with a high probability can be achieved by choosing a matrix A with random elements distributed, for example, according to the normal law or Bernoulli's law (randomization of the process). Random matrices are largely incoherent with any fixed basis Ψ [Bourgain et al., 2011]. The less coherence, the less M can be. But random matrices are not optimal or stable and other methods are often used [Gurbuz et al., 2009; Robucci et al., 2010].

Compression reduces the noise (small level noise), which in most cases has no sparse representation [Ben-Haim et al., 2010].

Whether the signal can be correctly restored from the compressed vector y depends on the measurement matrix, the compressed vector y itself and the reconstruction algorithm. Usually, ℓ_1 -optimization is used as a measure of the correspondence of the recovered signal to the original one or the size of the error. The reconstructed compressible signal $\hat{x} = \arg \min \|x\|_1$ will be correspond to the initial one with a high probability when $M \geq C_1 s \log(N/s)$, where C_1 is a constant depending on the method of creating the measurement matrix. This is a convex optimization problem, which can be considered as well as the linear programming problem, known as basis pursuit [Foucart, Rauhut, 2013]. To take into account data noise and transformations noise, use ℓ_1 -optimization with relaxed constraints: $\min \|x\|_1$: $\|A\hat{x} - y\|_2 \leq \epsilon$, where ϵ describes noise. Other algorithms are used for recovery too [Blumensath, Davies, 2009].

The recovery error consists of two components: the first is proportional to the data noise, the second is the approximation error. The quality of reconstruction considerably decreases with increasing the noise. It is possible to estimate the error on a wide range of parameters only by comparing the original and restored seismograms (Fig. 1).

Many types of analysis are possible without signal reconstruction [Davenport et al., 2010]. This removes the recovery error. For example, the CS algorithm can easily be embedded into the neural network as an extra layer [Li et al., 2018].

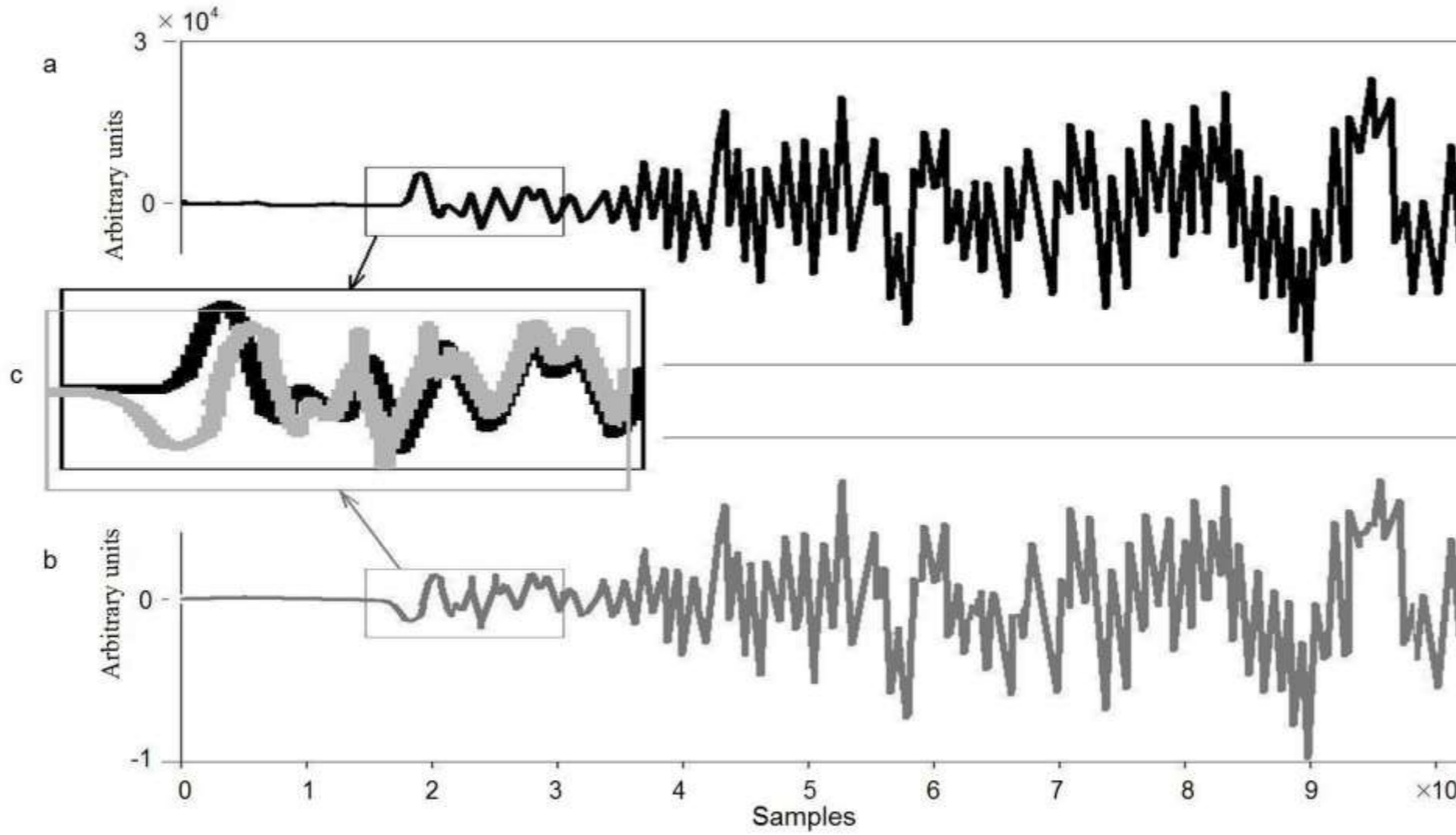


Fig. 1 a - the first arrival of the earthquake; b - an example of signal recovery; $N = 1024$, $M = 60$; c - the comparison.

CS is increasingly used in seismic exploration works and data processing of seismic networks [Yao et al., 2011; Herrmann, 2019].

CS-method is a very effective. But its main advantages will be affected when seismic sensors will take random observations. The obstacles to using CS as the seismic data pre-processing are the requirement of low noise and the need for high sparsity [Davenport et al., 2012]. In addition CS algorithms have large computational costs and their application is difficult in real-time systems.

COMPRESSION CODING WITH TRANSFORMATION

For audio and video compression, coding with transformation is used, which also uses s -sparse representations. A discrete wavelet transform (DWT), discrete Fourier transform (DFT) or discrete cosine transform (DCT) are commonly used for coding with transformation.

Even at small s , the use of these algorithms requires a large computational cost. All N transform coefficients must be calculated, but most of them (excluding s each) are useless. The values of s and the numbers of their positions in the vector w must be encoded [Granichin, Pavlenko, 2010]. Compression coding with transformation clearly loses over CS.

AUTOENCODER

In recent years, interest in autoencoders (AE) has increased again [Creswell, Bharath, 2019; Shi et al., 2019]. In [Valentine, Trampert, 2012], AE was used to compress seismic signals of a length of 512 counts into a 32-dimensional vector.

The simplest AE is a neural network with one hidden layer, trained by the back-propagation method to reconstruct its own inputs ($y = x$). The input x is mapped to the latent variable layer $z = h_1(Wx + \beta_0)$. Then z is mapped to the output layer $y = h_2(Wz + \beta_1)$. Here h is the element-by-element activation function (for example, a sigmoidal function, a ReLU, or another); adjustable parameters: β is bias weights, W is weight matrix. The AE is trained to minimize recovery errors (for example, root-mean-square error) $E(x, y) = \|x - y\|_2 = \|x - h_2(W(h_1(Wx + \beta_0)) + \beta_1)\|_2$ and is the input data mining tool. [Kislov, Gravirov, 2017]. Like principal component analysis (PCA), the AE translates data to a low dimensionality, but the transformation is non-linear. The AE is more promising than PCA or other known methods.

Deep AE can compress the data better. Let's define an exit of layer i as z_i , $i \in \{1, \dots, q+1\}$. At that, $z_0 \equiv x$; $y = z_{q+1}$, where q is the number of hidden layers. Then $z_i = h_i(z_{i-1}W_i + \beta_i)$. Usually deep AE contains 5 - 7 layers. In our case, layer sizes are 1000, 500, 250, 60, 250, 500, 1000 neurons. The middle layer, the 60-dimensional vector, is the compressed representation of the signal.

AE's education needs to adjust the matrix W and the biases β to minimize some loss function $L(x, y)$. The process is simplified if the symmetric autoencoder is used, i.e. the encoding and decoding weight matrices are transposed for each other $W_i = W_i^T$. On the other hand, if you abandon this principle, you can reduce the error of signal reconstruction [Majumdar, Tripathi, 2017].

We are interested in Stacked Denoising Autoencoder (SDAE) which has the possibility of data compression with noise reduction. When training, an artificially noisy signal is inputted. Noise is made out as adding Gaussian noise or a random process of zeroing some of the inputs. This forces AE to reveal the strongest interrelations, at the same time not building identical maps.

Training of deep AE can be solved using a greedy layer-by-layer algorithm and unlabeled data, i.e., unsupervised learning. For long, it was assumed that these are frills, and that the random initialization of the weights, the use of the ReLU activation function, and some tricks give the chance to train network by fine-tuning only. Only that's not enough in order to get the maximum effect from AE [Erhan et al., 2010].

A well-trained AE with an enhanced denoising version can solve many important seismological tasks. However, it does not provide effective suppression of various anthropogenic noises. The trained AE works for orders quicker than CS.

WAVELET TRANSFORM

The wavelet transform is a convolution of the analyzed signal $x(t)$, $t \in (-\infty, \infty)$ with wavelet functions $\psi\left(\frac{t-b}{a}\right)$, $a, b \in (-\infty, \infty)$, $a \neq 0$ [Saad et al., 2019]. Seismic data $x_k = x(t_k)$ is a time series of consecutive values with a constant step Δt : $t_k = \Delta t \cdot k$, $k = 0, 1, \dots, N-1$. Their discrete wavelet transformation is defined by the following expression:

$$W(a, b) = \frac{1}{n(a, b)} \sum_{k=0}^{N-1} x_k \psi\left(\frac{t_k - b}{a}\right), \quad n(a, b) = \sum_{k=0}^{N-1} \psi^2\left(\frac{t_k - b}{a}\right),$$

where $a, b \in R$; $a \neq 0$; $x(t)$ is the signal; $\psi(t)$ is the wavelet. The parameter a is scale. It determines the size of the wavelet function $\psi\left(\frac{t-b}{a}\right)$.

Its analogue in Fourier analysis is the period of harmonic oscillation. The value b is shift along the time axis.

It is convenient to use elements of the local energy spectrum or scalogram as the input to the DNN. At the bottom of the scalogram (Fig. 2) there are coefficients with small numbers, giving a detailed picture of the signal, and from above - with large numbers, giving a coarse picture of the signal.

In Fig. 2a you can clearly see added complexity of the spectrum at the edges. We have developed an algorithm that implements an adaptive filter bandwidth selection and allows processing and filtering of input digital seismic data [Gravirov et al., 2014]. You can isolate the interfering low-frequency components and the splashes associated with technogenic noise and remove them from the original process (see Fig. 2b). We have stopped at fourth-order Daubechies wavelets "db4". If using them, the form of the reconstructed signal is the least different from the original.

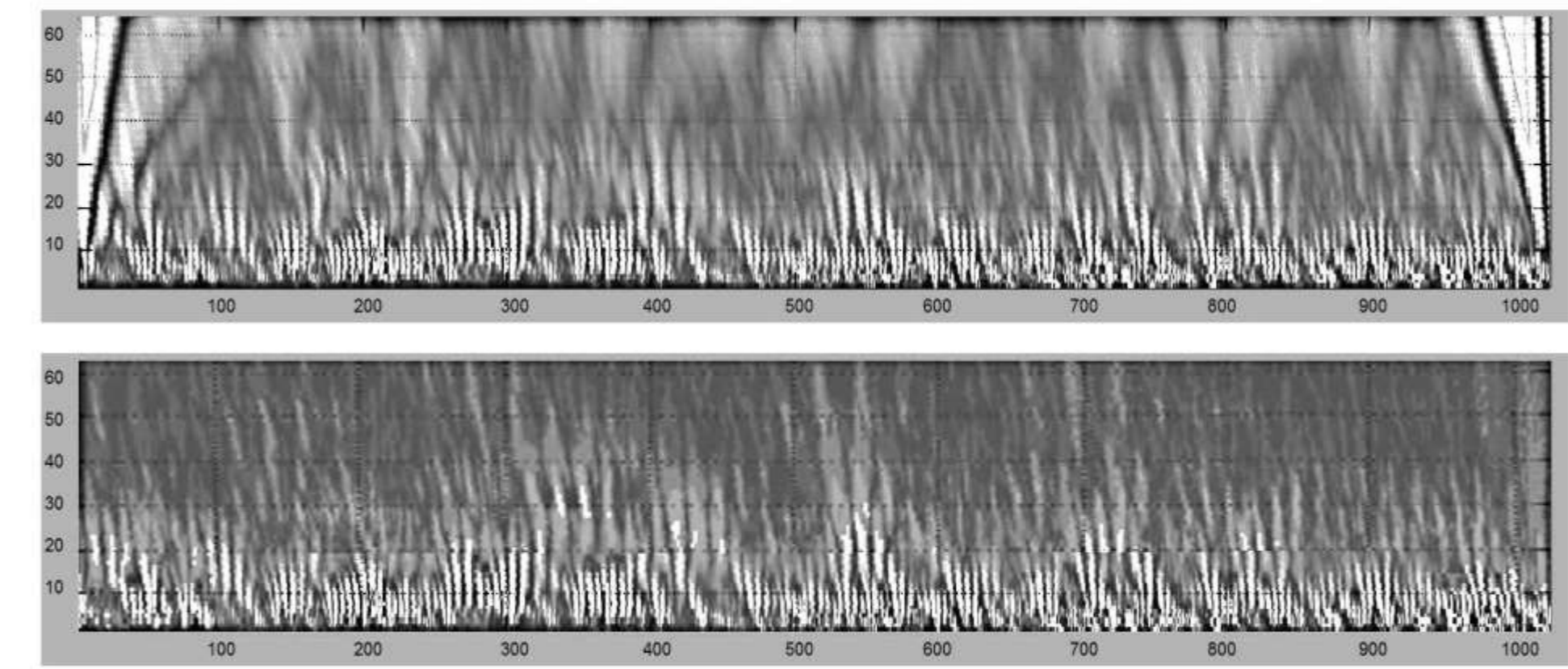


Fig. 2. Representation of a test seismic signal with a depth of decomposition of 64: a - the scalogram of the seismic window with a length of 1024 samples; b - processed scalogram of the same section of the recording.

Usually for further processing choose 5-8 the most characteristic levels of decomposition. The spectral bands can be selected based on the power distribution [Altunkaynak, 2014]. Decomposition on each band is a kind of signal feature map. Reconstruction of a signal according to feature maps gives the signal cleaned from noise. Reconstruction by one of the feature maps makes it possible to consider the features highlighted by this card (Fig. 3).

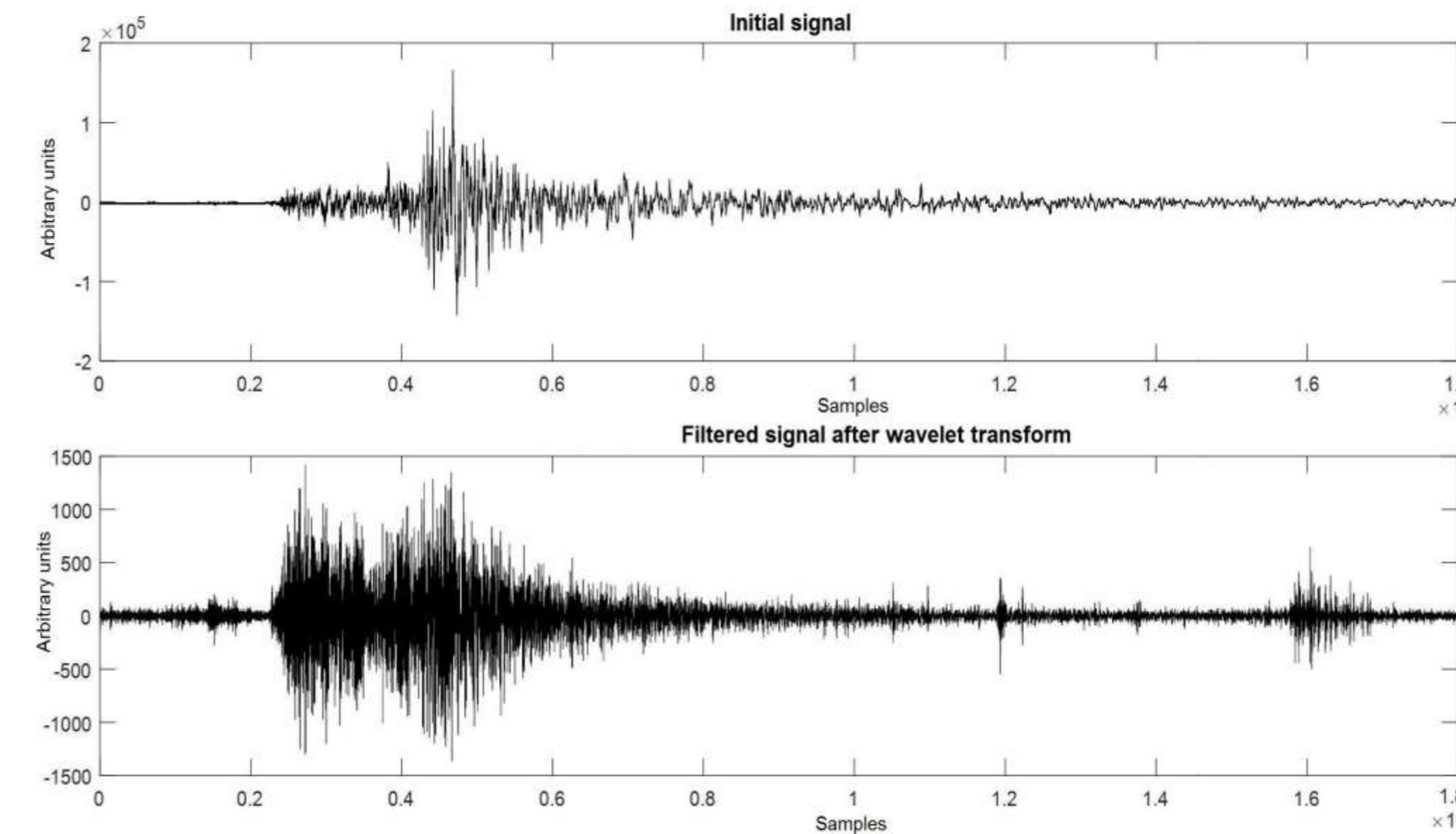


Fig. 3. a - Earthquake recording; b - The same signal, restored after the wavelet transform by feature map number 64.

The approach when the wavelet transformation applies to feature extraction is quite useful if you use the convolutional layer as the input of the DNN.

CONCLUSION

We have explored the most promising methods, although there may be other approaches. It is not possible to make certain conclusions on the effectiveness or ineffectiveness of this or that method due to the diversity of seismological tasks, especially since new tasks may appear. The coding part of AE compresses data well, but loses in noise reduction. The wavelet as data pre-processing increases the input data for DNN, but well marks out features of a signal. CS eliminates the "symmetrical" noise and compresses the data well, but requires additional control of saving information.

At reconstruction of a signal, the error of recovery is added, and the computational cost increases. It is better to use reconstruction only for visualization and control, and to work only with the transformed data. Only the noise components of the recordings are subject to removal: instrumental and technogenic noise.

The seismic data pre-processing is necessary not only for the analysis by the DNN, but also for other methods of analysis.

It seems to us that with the present level of development of the DNN, the preferred method of seismic recordings pre-processing is the wavelet transformation. In addition to the excellent ability of this method to filter noises of various nature, it allows to clearly localize the signal changes over time, and it very visual method.

The purpose of this work was comparison of various methods for seismic data pre-processing and providing reference materials for future research.

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