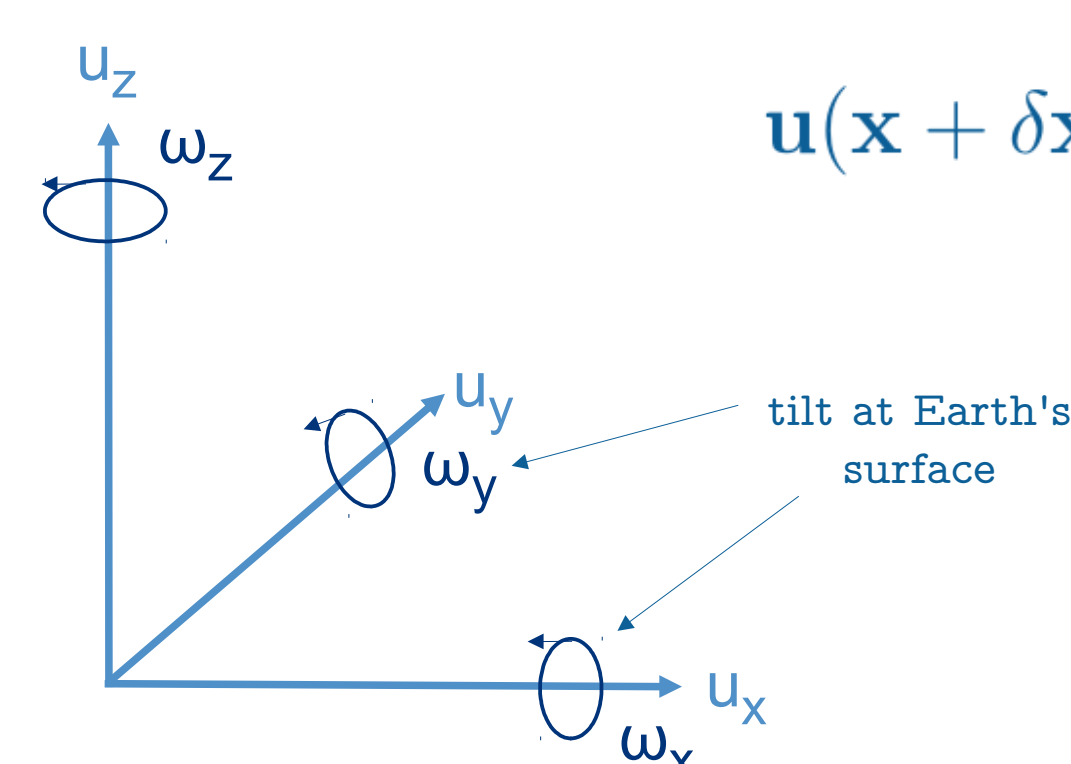




Questions

What are rotational ground motions?

Assuming an infinitesimal deformation within an elastic medium, the entire wavefield due to a seismic source is described by 12 components.



$$\mathbf{u}(\mathbf{x} + \delta\mathbf{x}) = \mathbf{u}(\mathbf{x}) + \epsilon \cdot \delta\mathbf{x} + \omega \times \delta\mathbf{x}$$

translation strain rotation

$$\omega(\mathbf{x}, t) = \frac{1}{2} [\nabla \times \mathbf{u}(\mathbf{x}, t)]$$

- information on the vertical displacement gradient
- not available from conventional arrays on Earth's surface

How can they serve CTBT?

In very manifold ways. Follow the red line.

All methods shown are **single station approaches**. Test case is the Mw 7.2 Tajikistan earthquake from 7 December 2015 measured at the ringlaser in Wettzell, Germany, recording vertical rotation rate.

How does the magic work?

By collocated measurement. Assume a plane SH/Love wave in X direction.

velocity
 $\dot{u}_y = \dot{u}_y \sin(kx - \omega t)$

acceleration
 $\ddot{u}_y = -\dot{u}_y \omega \cos(kx - \omega t)$

rotation rate
 $\dot{\omega}_z = -\frac{1}{2} \dot{u}_y k \cos(kx - \omega t)$

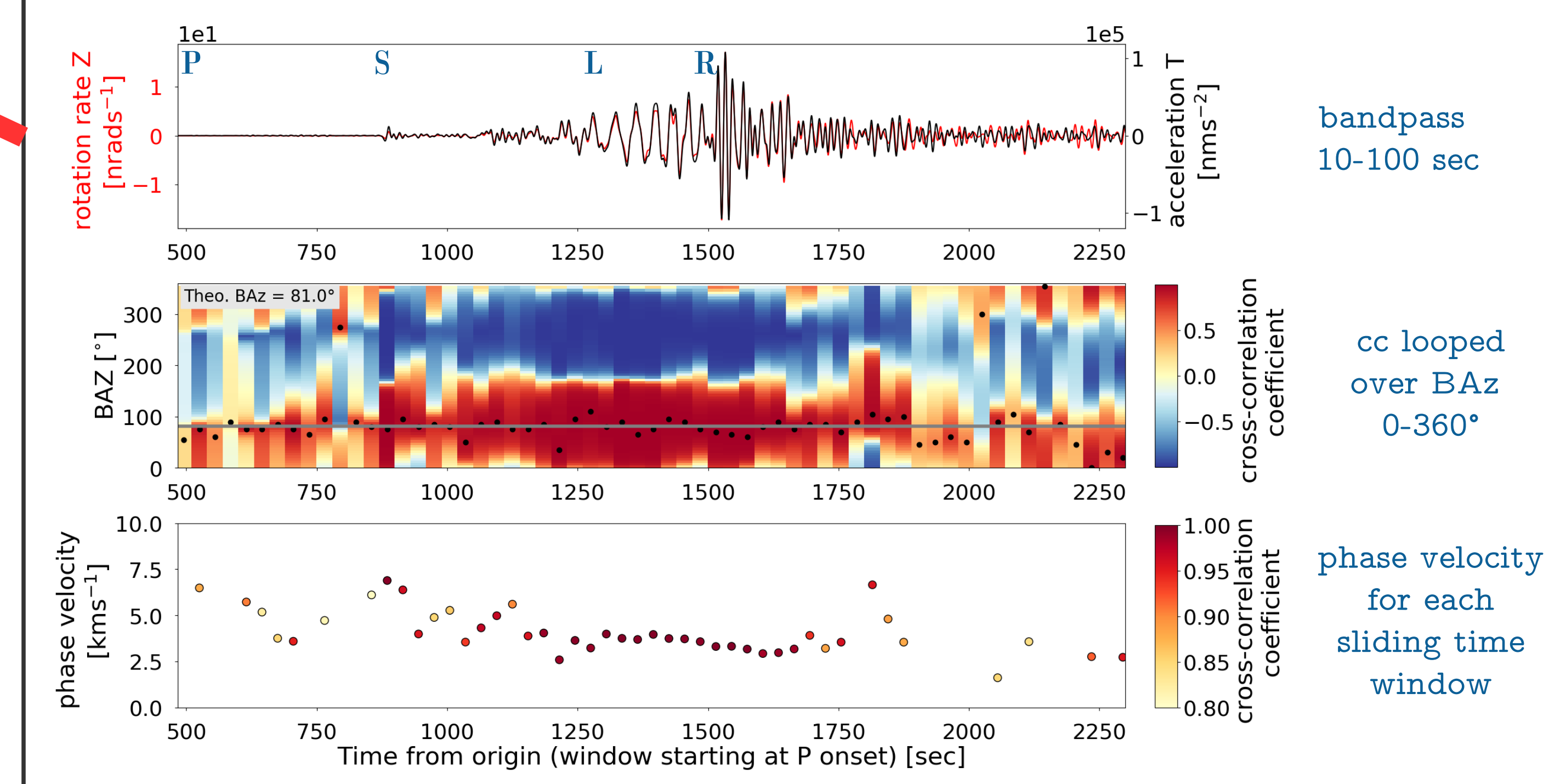
local phase velocity
 $\frac{\dot{u}_y}{\dot{\omega}_z} = -2c$

similarly for Rayleigh waves: $\frac{\ddot{u}_z}{\dot{\omega}_y} = c$

Rotational ground motion components act as wavetype filters!

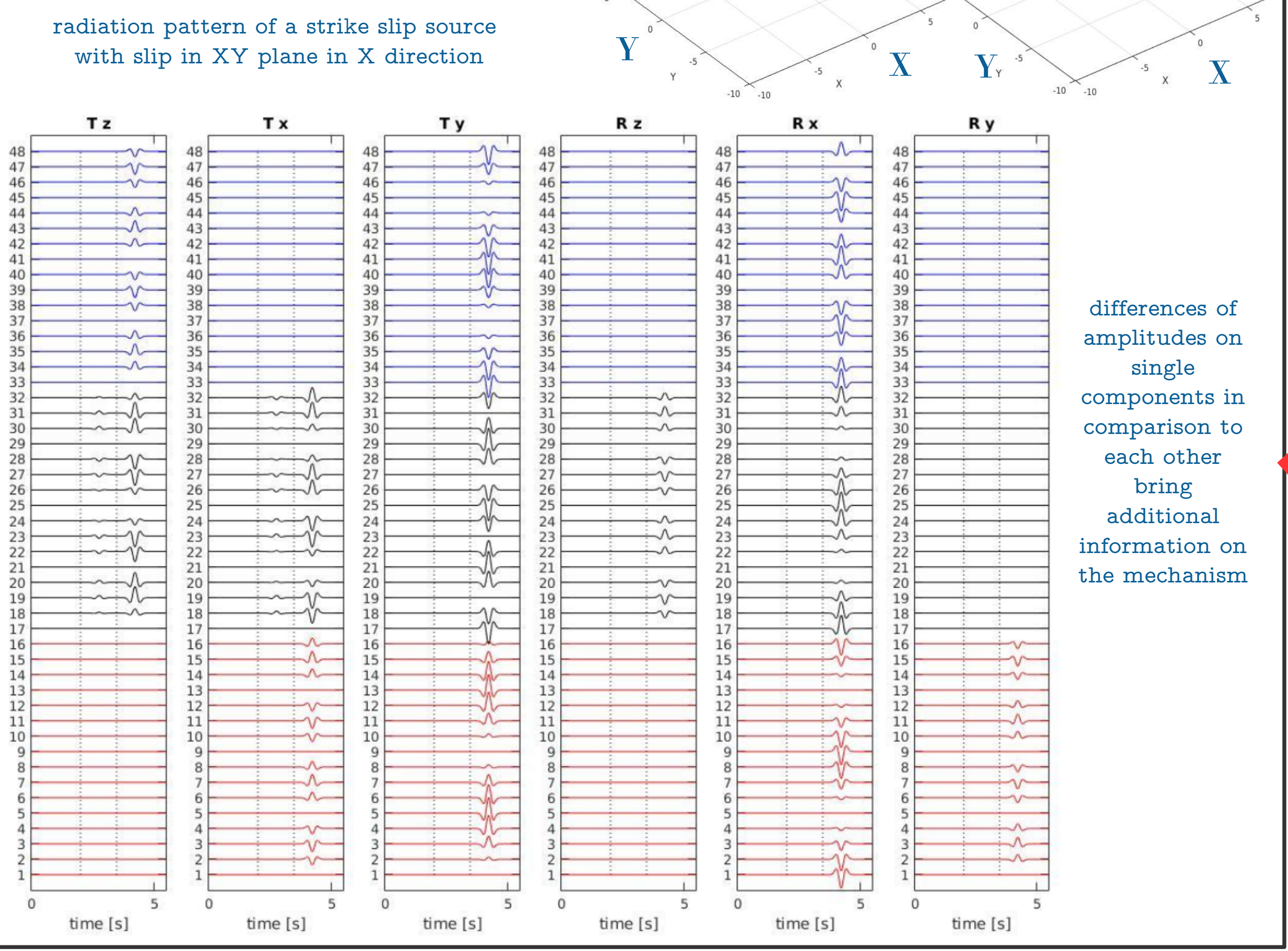
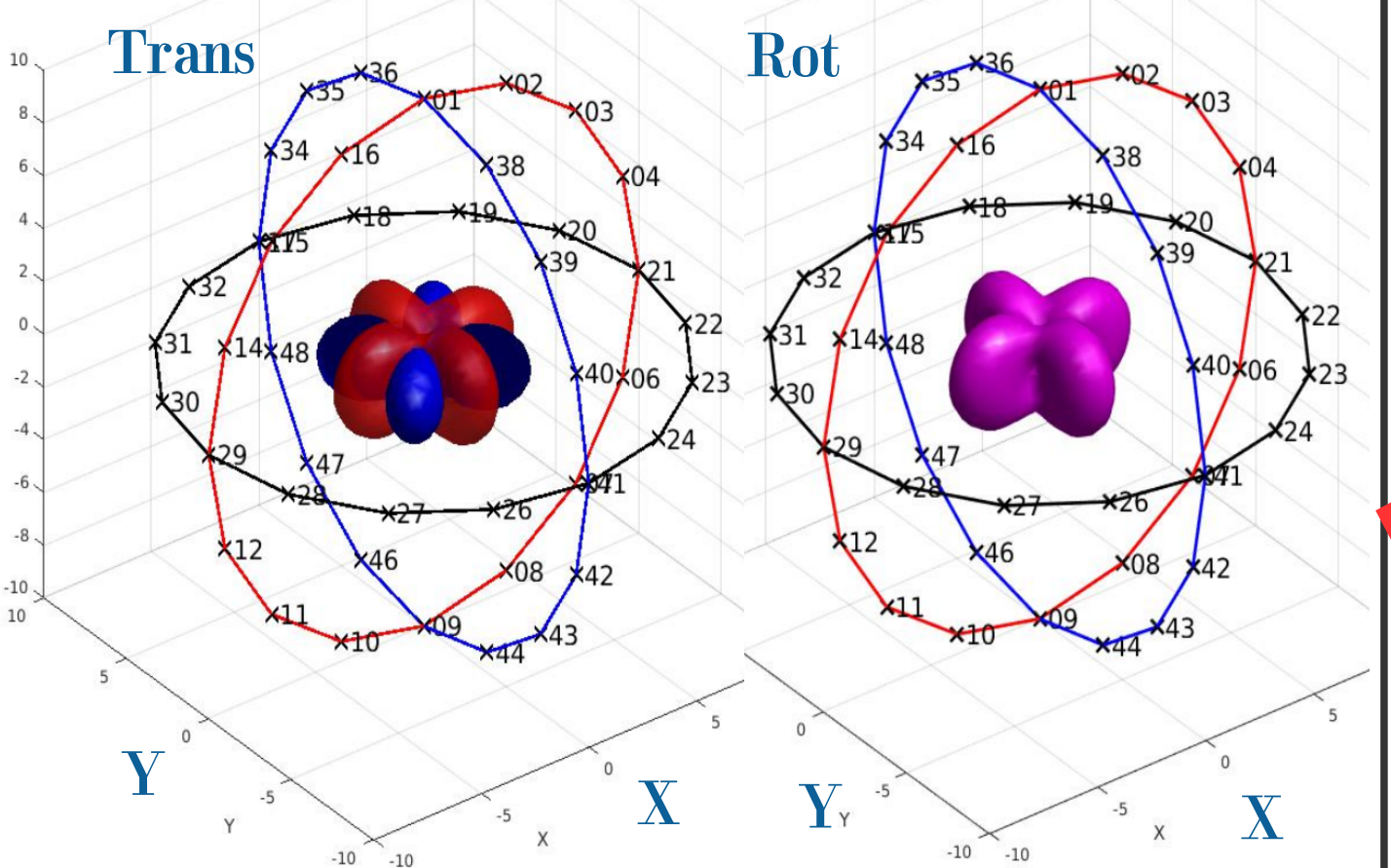
Get direction and local phase velocity

Cross-correlation of translation and rotation in sliding time window (30 sec)



Source discrimination

Was it an explosion or tectonic? Wavetype filter effect of rotations compared with translations may help to decide.



Earthquake location (without knowing model)

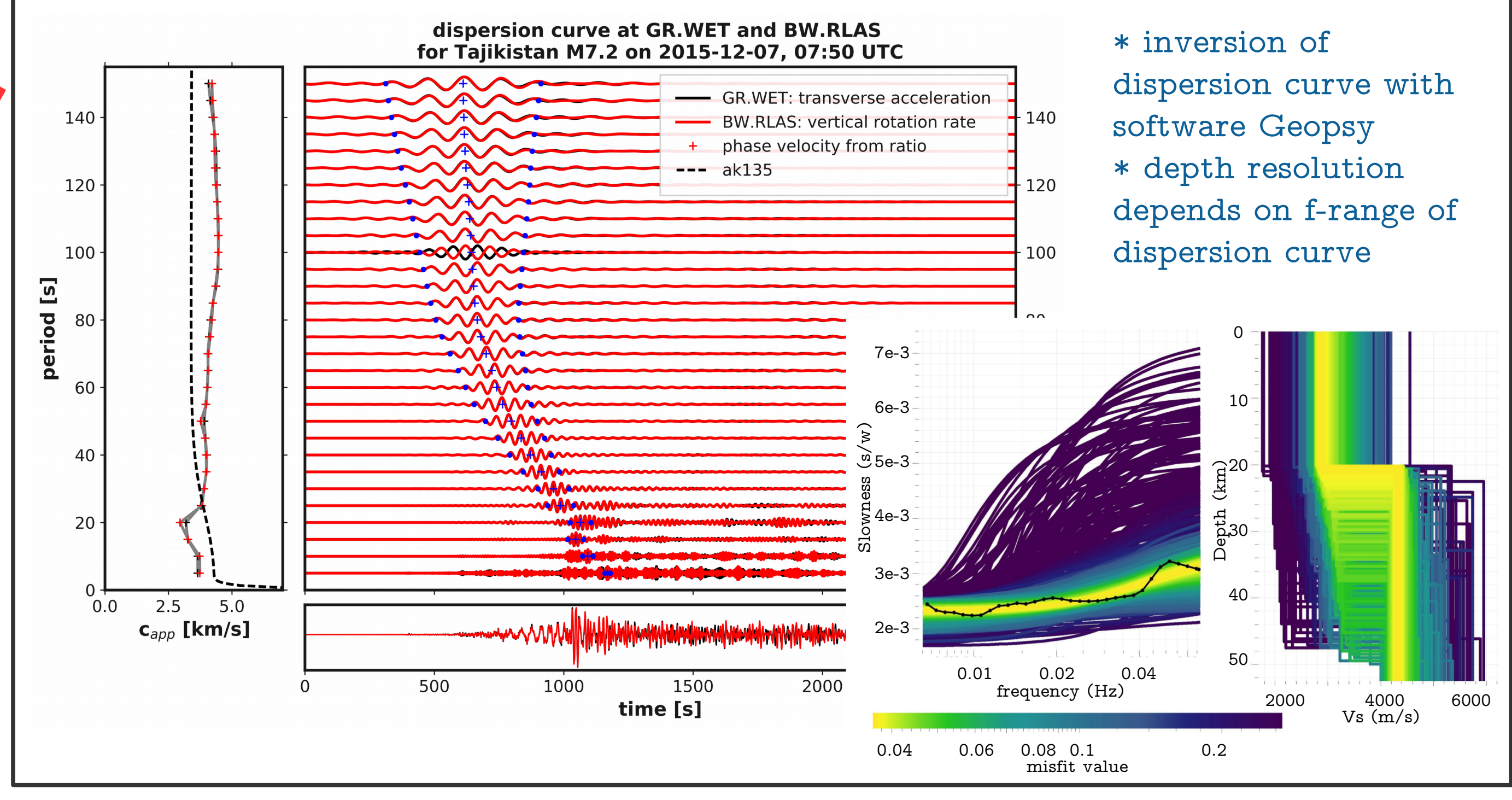
	IRIS	3C	4C
travel time difference [s]	388	392	390
source time UTC [h:m:s]	07:50:05	07:50:04	07:50:06
distance [°]	43.48	44.05	43.70
distance [km]	4834	4898	4859
latitude [°]	38.21	44.54	38.71
longitude [°]	72.77	80.41	73.55
backazimuth [°]	81	69 (55-81)†	80 (60-95)†
depth [km]	22	-	20-35

- get S-P arrival time → distance
- get P arrival from distance → origin time
- get BAZ from CC → location
- get v-model from dispersion curve inversion
- get rough depth estimate via ray-tracing; backshooting and comparing incident angle via:

$$\text{from model } \frac{v_S}{v_{Sapp}} = \sin i \pm \epsilon = \frac{180}{\pi} \cdot \frac{v_P}{v_h} \cdot p(\Delta, h)$$

Get local structure via dispersion curve

Get amplitude ratios in different frequency/period bands (cc with real BAZ)



Summary (not everything shown here)

- Structural engineering**
 - torsional modes
 - interstory drift
 - ...
- Structure**
 - phase velocity
 - dispersion curve
 - shallow surface structure
 - sensitivity kernels
 - toroidal mode
- Wavefield**
 - wavefield separation
 - wavetype ratios
 - scattering
 - tilt (OBS)
- Exploration**
 - wavefield characterization
 - wavefield reconstruction
 - P-S separation in VSP
 - surface wave suppression
- Source**
 - direction, location
 - source discrimination
 - microseism, earthquakes
 - inversion for mechanism

References

* Schmelzbach, C., Donner, S., Igel, H., Sollberger, D., Taufiqurrahman, T., Bernauer, F., Häusler, M., Renterghem, C. V., Wassermann, J. & Robertsson, J. (2018) *Advances in 6C seismology: Applications of combined translational and rotational motion measurements in global and exploration seismology*. GEOPHYSICS, vol. 83, pp. WC53-WC69. ... and references therein.

* <http://romy-erc.org> → Publications